



BIRZEIT UNIVERSITY

**BIRZEIT UNIVERSITY**  
**Faculty of Engineering**  
**Electrical Engineering Department**  
*Network Analysis II - ENEE335*  
**Final Exam**

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**Problem #1(25 pts) :**

The z and y parameters for the resistive two-ports in figure 1 are given by

$$z = \begin{bmatrix} \frac{35}{3} \Omega & -\frac{100}{3} \Omega \\ \frac{4}{3} \text{k}\Omega & \frac{10}{3} \text{k}\Omega \end{bmatrix} \quad y = \begin{bmatrix} 200 \mu\text{S} & 40 \mu\text{S} \\ -800 \mu\text{S} & 40 \mu\text{S} \end{bmatrix}$$

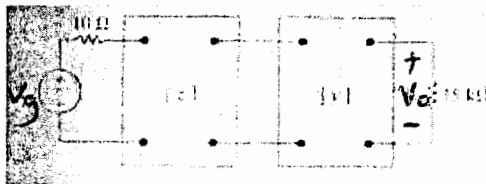


Fig 1

Calculate  $v_o$  if  $v_g = 30 \text{mV dc}$

**Problem #2 (25 pts):**

- a. Design a circuit to realize the transfer function below using only resistors, capacitors, and not more than one OP AMP. Scale the circuit so that all capacitors are exactly 100 pF

$$H(s) = \frac{100(s + 500)}{(s + 200)(s + 2500)}$$

- b. For the circuit shown in figure 2

$$= \frac{c \cdot 1 \left(1 + \frac{s}{500}\right)}{\left(1 + \frac{s}{200}\right) \left(1 + \frac{s}{2500}\right)}$$

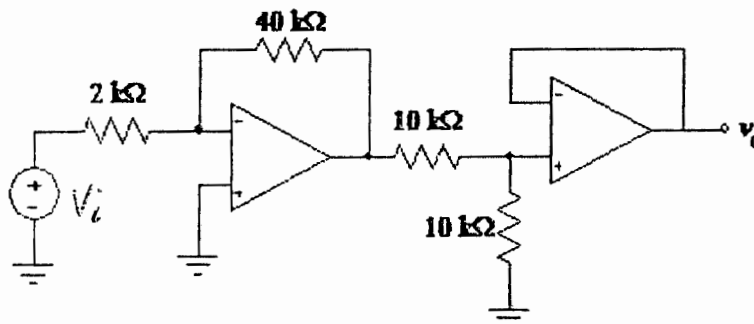


Fig 2

Find  $H(s) = \frac{v_o}{v_{in}}$

Handwritten calculations:

$$\frac{2v_o}{v_i} = -20$$

$$\frac{v_o}{v_i} = -10$$

**Problem #3 (25 pts):**

a. For the following gain bode plot shown in figure 3 .

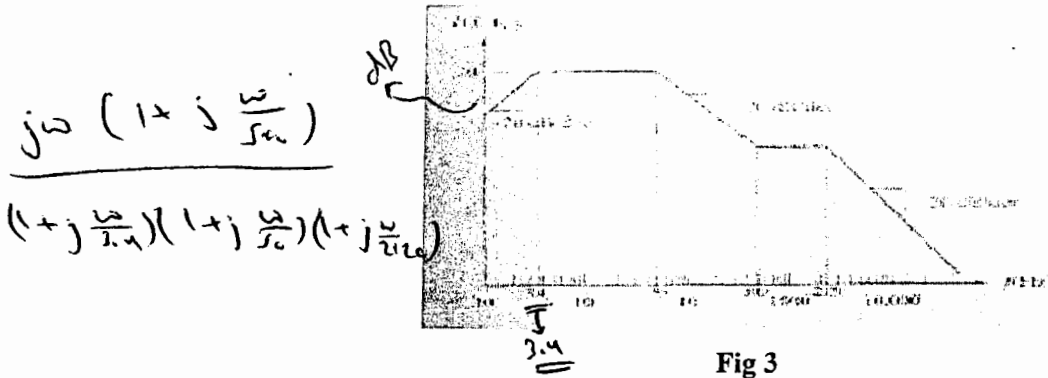


Fig 3

1. Construct a transfer function  $H(s)$
  2. Design an active RC circuit to realize the  $H(s)$  found in (1).
- b. Construct a plot of the straight-line approximation to the gain response for the following transfer function

$$H(s) = \frac{4(s + 300)}{(s + 20)(s + 60)}$$

**Problem #4 (25 pts):**

a. For the following circuit shown in figure 4

Handwritten transfer function:

$$\frac{R}{R + \frac{1}{Cs} + \frac{Ls}{R}} = \frac{R^2 Cs}{R^2 Cs + R + Ls}$$

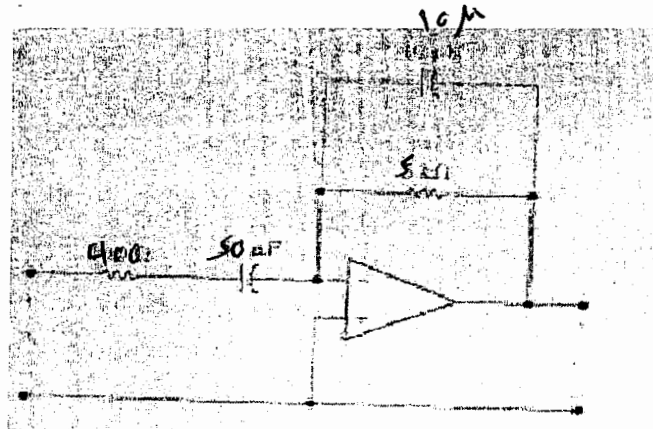


Fig 4

1. Show that the circuit behaves as bandpass filter
  2. Find the center frequency, bandwidth and gain for this filter
  3. Find the cutoff frequencies and the quality for this filter
- b. Determine the order of a low-pass Butterworth filter that has a cutoff frequency of 2000 Hz and a gain of no more than -30dB at 7000 Hz

Handwritten notes:

$$A_s = \frac{10.02}{\log(\frac{7000}{2000})}$$

GOOD LUCK ☺

## Relationships Among the Two-Port Parameters

Because the six sets of equations relate to the same variables, the parameters associated with any pair of equations must be related to the parameters of all the other pairs. In other words, if we know one set of parameters, we can derive all the other sets from the known set. Because of the amount of algebra involved in these derivations, we merely list the results in Table 18.1.

TABLE 18.1 Parameter Conversion Table

$z_{11} = \frac{v_{22}}{\Delta y} = \frac{a_{11}}{a_{21}} = \frac{b_{22}}{b_{21}} = \frac{\Delta h}{h_{22}} = \frac{1}{g_{11}}$	$b_{21} = \frac{1}{z_{12}} = -\frac{\Delta y}{y_{12}} = \frac{a_{21}}{\Delta a} = \frac{h_{22}}{h_{12}} = -\frac{g_{11}}{g_{12}}$
$z_{12} = -\frac{y_{12}}{\Delta y} = \frac{\Delta a}{a_{21}} = \frac{1}{b_{21}} = \frac{h_{12}}{h_{22}} = -\frac{g_{12}}{g_{11}}$	$b_{22} = \frac{z_{11}}{z_{12}} = \frac{y_{22}}{y_{12}} = \frac{a_{11}}{\Delta a} = \frac{\Delta h}{h_{12}} = -\frac{1}{g_{12}}$
$z_{21} = \frac{-y_{21}}{\Delta y} = \frac{1}{a_{21}} = \frac{\Delta b}{b_{21}} = -\frac{h_{21}}{h_{22}} = \frac{g_{21}}{g_{11}}$	$h_{11} = \frac{\Delta z}{z_{22}} = \frac{1}{y_{11}} = \frac{a_{12}}{a_{22}} = \frac{b_{12}}{b_{11}} = \frac{g_{22}}{\Delta g}$
$z_{22} = \frac{y_{11}}{\Delta y} = \frac{a_{22}}{a_{21}} = \frac{b_{11}}{b_{21}} = \frac{1}{h_{22}} = \frac{\Delta g}{g_{11}}$	$h_{12} = \frac{z_{12}}{z_{22}} = -\frac{y_{12}}{y_{11}} = \frac{\Delta a}{a_{22}} = \frac{1}{b_{11}} = -\frac{g_{12}}{\Delta g}$
$y_{11} = \frac{z_{22}}{\Delta z} = \frac{a_{22}}{a_{12}} = \frac{b_{11}}{b_{12}} = \frac{1}{h_{11}} = \frac{\Delta g}{g_{22}}$	$h_{21} = -\frac{z_{21}}{z_{22}} = \frac{y_{21}}{y_{11}} = -\frac{1}{a_{22}} = -\frac{\Delta b}{b_{11}} = -\frac{g_{21}}{\Delta g}$
$y_{12} = -\frac{z_{12}}{\Delta z} = -\frac{\Delta a}{a_{12}} = -\frac{1}{b_{12}} = -\frac{h_{12}}{h_{11}} = \frac{g_{12}}{g_{22}}$	$h_{22} = \frac{1}{z_{22}} = \frac{\Delta y}{y_{11}} = \frac{a_{21}}{a_{22}} = \frac{b_{21}}{b_{11}} = \frac{g_{11}}{\Delta g}$
$y_{21} = \frac{z_{21}}{\Delta z} = \frac{1}{a_{12}} = -\frac{\Delta b}{b_{12}} = \frac{h_{21}}{h_{11}} = -\frac{g_{21}}{g_{22}}$	$g_{11} = \frac{1}{z_{11}} = \frac{\Delta y}{y_{22}} = \frac{a_{21}}{a_{11}} = \frac{b_{21}}{b_{22}} = \frac{h_{22}}{\Delta h}$
$y_{22} = \frac{z_{11}}{\Delta z} = \frac{a_{11}}{a_{12}} = \frac{b_{22}}{b_{12}} = \frac{\Delta h}{h_{11}} = \frac{1}{g_{22}}$	$g_{12} = -\frac{z_{12}}{z_{11}} = \frac{y_{12}}{y_{22}} = -\frac{\Delta a}{a_{11}} = -\frac{1}{b_{22}} = -\frac{h_{12}}{\Delta h}$
$a_{11} = \frac{z_{11}}{z_{21}} = \frac{y_{22}}{y_{21}} = \frac{b_{22}}{\Delta b} = \frac{\Delta h}{h_{21}} = \frac{1}{g_{21}}$	$g_{21} = \frac{z_{21}}{z_{11}} = -\frac{y_{21}}{y_{22}} = \frac{1}{a_{11}} = \frac{\Delta b}{b_{22}} = -\frac{h_{21}}{\Delta h}$
$a_{12} = \frac{\Delta z}{z_{21}} = -\frac{1}{y_{21}} = \frac{b_{12}}{\Delta b} = \frac{h_{11}}{h_{21}} = \frac{g_{22}}{g_{21}}$	$g_{22} = \frac{\Delta z}{z_{11}} = \frac{1}{y_{22}} = \frac{a_{12}}{a_{11}} = \frac{b_{12}}{b_{22}} = \frac{h_{11}}{\Delta h}$
$a_{21} = \frac{1}{z_{21}} = -\frac{\Delta y}{y_{21}} = \frac{b_{21}}{\Delta b} = -\frac{h_{22}}{h_{21}} = \frac{g_{11}}{g_{21}}$	$\Delta z = z_{11}z_{22} - z_{12}z_{21}$
$a_{22} = \frac{z_{22}}{z_{21}} = -\frac{y_{11}}{y_{21}} = \frac{b_{11}}{\Delta b} = -\frac{1}{h_{21}} = \frac{\Delta g}{g_{21}}$	$\Delta y = y_{11}y_{22} - y_{12}y_{21}$
$b_{11} = \frac{z_{22}}{z_{12}} = -\frac{y_{11}}{y_{12}} = \frac{a_{22}}{\Delta a} = \frac{1}{h_{12}} = -\frac{\Delta g}{g_{12}}$	$\Delta a = a_{11}a_{22} - a_{12}a_{21}$
$b_{12} = \frac{\Delta z}{z_{12}} = -\frac{1}{y_{12}} = \frac{a_{12}}{\Delta a} = \frac{h_{11}}{h_{12}} = -\frac{g_{22}}{g_{12}}$	$\Delta b = b_{11}b_{22} - b_{12}b_{21}$
	$\Delta h = h_{11}h_{22} - h_{12}h_{21}$
	$\Delta g = g_{11}g_{22} - g_{12}g_{21}$

Although we do not derive all the relationships listed in Table 18.1, we do derive those between the  $z$  and  $y$  parameters and between the  $z$  and  $a$  parameters. These derivations illustrate the general process involved in relating one set of parameters to another. To find the  $z$  parameters as functions of the  $y$  parameters, we first solve Eqs. 18.2 for  $V_1$  and  $V_2$ .